Abstract

We report a study of the structural and electrical properties of a carboxylic acid derivative (CAD) with structural formula C_5H_8O_2 ((E)-pent-2-enoic acid). Using the Møller-Plesset Perturbation Theory (MP2) and the Density Functional Theory (DFT/CAM-B3LYP) with the 6-311++G(d,p) basis set the dipole moment, the linear polarizability and the first and second hyperpolarizabilities are calculated in presence of static and dynamic electric field. Through the supermolecule approach the crystalline phase of the carboxylic acid derivative is simulated and the environment polarization effects on the electrical parameters are studied. Static and dynamic estimation of the linear refractive index and the third-order nonlinear susceptibility of the crystal are obtained and compared with available experimental results. The characteristic vibrational modes and functional groups present in CAD were analyzed by Fourier Transform Infrared Spectrum (FT-IR) in the region of 400–4000 cm⁻¹. Through the Hirshfeld surface analysis the molecular structure and the vibrational modes properties of the CAD crystal are explored. The effects of solvent medium on the molecular properties are taken into account through the Polarizable Continuum Model (PCM). Also, the frontiers molecular orbitals, the band gap energy, and the global chemical reactivity descriptors are discussed. All the properties studied suggest that the present material may be considered for nonlinear optical material.

Keywords: First and second hyperpolarizabilities; Hirshfeld surface analysis; third-order susceptibility

1. Introduction

In recent decades, organic compounds have attracted great attention motivated by their potential applications in chemistry of materials such as nonlinear optical materials (NLO), solar cell materials, photonic materials, photonic devices, optical devices, electrochemical sensors, in ultra-fast optical signal processing. Due to architectural flexibility and ease of manufacturing the NLO devices, organic materials with extensively delocalized π electrons have attracted significant attention due to their large NLO susceptibility. The advantage of the organic compounds over the inorganic materials is that NLO properties can be manipulated, by changing the substituents and the functional groups on the starting reactants. The NLO response of the organic compounds to the action of an applied electric field is related to the relocation of the π-electron.
Finding new organic crystals that present efficient NLO properties is the challenge of the present days and a great number of experimental and theoretical works has been addressed to this end. In this context, here we present an investigation of the electric and optical properties of a carboxylic acid derivative. Carboxylic acid derivatives have various applications in textile treatment, in the production of cellulose plastics and ester; as an example the ester of salicylic acid is prepared from acetic acid. The use of unsaturated fatty acids and fatty acids in general have been used with great interest in nutrition and health sciences, due to their great role in biological processes, especially as an antibiotic against many bacteria and fungi. Fatty acids and their derivatives act as a receptor ligand in the cerebral cortex and hippocampus and elevated concentrations can be found in patients with Alzheimer’s and Parkinson’s disease. Determinations of the crystal structure of α,β-unsaturated carboxylic acids are still scarce in the literature, but in recent years it has been gaining great interest from researchers. Our motivation for the study of α,β-unsaturated carboxylic acid crystal came from the fact that we not found works in the literature that treat of the NLO properties of this material.

The constituent units of an organic crystal may possess (or not) a center of symmetry, which is responsible for nonlinear optical effects, as well as by the generation of the second and third susceptibility governed respectively by the first and second hyperpolarizabilities. Density functional theory (DFT) and other methods in quantum chemistry have proved to be highly successful in describing structural and electronic properties, as the molecular polarizabilities and hyperpolarizabilities, static and dynamic in a vast class of materials from atoms and molecules to simple crystals. The carboxylic acid derivative (CAD) studied in this work is the (E)-pent-2-enoic acid with structural formula C₅H₈O₂ (Figure 1); it was synthesized and structurally characterized by Tim Peppel et al. Through an ab initio approach the dipole moment, the linear polarizability and the dipole moment was the calculation of the gap energies calculated in presence of several solvent media.

2. Methodology

2.1. Hirshfeld Surface

The CAD compound was crystallized, in a triclinic centrosymmetric space group P1 with the following crystallographic data: a = 6.7336 (13) Å, b = 6.7821 (13) Å, c = 7.2349 (14) Å, α = 67.743 (2)°, β = 75.518 (2)°, γ = 64.401 (2)°, unit cell volume V = 274.29 (9) Å³ with 2 molecules in the unit cell. The (E)-pent-2-enoic acid is essentially planar.

The intermolecular interactions and their quantitative contributions to the stability of supramolecular assemble in organic crystals of CAD can be explored by Hirshfeld surface analysis and the associated 2D-fingerprint plots was calculated using Crystal Explorer software. These tools allow us to examine the context of the whole system through the color mapping identifying specific regions where the intermolecular interactions occur; these tools also allow to quantify percentage of areas related to each contact. Fingerprint plots can summarize all contact distances to the Hirshfeld surface and express their contributions in terms of a percentage share.

![Figure 1: A view of the asymmetric unit of the compound C₅H₈O₂ with the atom-numbering scheme.](image)

2.2. Computational Details

The theoretical method used to calculate the static linear polarizability and the dipole moment was the Moller-Plesset Perturbation Theory (MP2). The other parameters as the hyperpolarizabilities were calculated via the Density Functional Theory (DFT) with CAM-B3LYP functional. In all calculations the 6-31+G(d,p) basis set was used took. The SM approach taken into account the crystallographic geometry obtained by X-ray by Tim Peppel et al. Previous studies have shown that this basis set provide a realistic description of the electrical properties.

The crystalline environment polarization was simulated by the supermolecule (SM) approach, where the atoms of the surrounding molecules are considered as point charge. The approach operates with a bulk consisting of a set of 11×11×11 unit cells, with 2 asymmetric units in each unit cell, totaling 1331 unit cells generating a bulk with 39,930 atoms. A schematic representation of this bulk is shown in Figure 2, where the CAD isolated molecule is highlighted in blue in the center of the image.

The SM approach have been used in several works, in Ref. the authors showed that this method can represent the dipole moment and the first hyperpolarizability with results close to those of the experimental ones. In Ref.
the authors have shown that the SM can represent macroscopic properties of the crystal as the linear susceptibility, $\chi^{(1)}$, and for the nonlinear second-order susceptibility, $\chi^{(2)}$, in this case they worked with urea and thiourea and their theoretical results were close to those of experiments, after using a scale factor. In Ref. 40 the authors also simulated the properties of $\chi^{(1)}$ and $\chi^{(2)}$ of the molecule 3-methyl-4-nitropyridine-1-oxyde with results again close to the experimental ones.

The iterative process of the SM approach is carried out in several steps: first we determined the electric charge of the isolated molecule, by adjusting the molecular electrostatic potential (ChelpG), considering the electric charges distribution in vacuum, through the MP2 method. The partial atomic charges of the single isolated molecule of an asymmetric unit are calculated (ChelpG). Then we replace each corresponding atom in the generated unit cells by the partial atomic charge, previously obtained, and the static electric properties (dipole moment ($\mu$), linear polarizability ($\alpha$) and first ($\beta$) second ($\gamma$) hyperpolarizabilities) and the new partial atomic charges of the asymmetric unit were calculated. The iterative process continues with the substitution of the partial atomic charges in each calculation step, until the convergence of the electric dipole moment be reached.

The applicability of the supermolecule approach and the scheme of electrostatic polarization is advantageous due to the rapid convergence of the dipole moment of CAD throughout the process, in which six iterations were considered. The convergence of iterative series for this electrical property can be seen in Figure 3.

In the present study the electronic dipole moment, molecular mean polarizability ($\langle \alpha \rangle$), anisotropy of polarizability ($\Delta \alpha$) and first ($\beta_{\text{total}}$) second ($\gamma$) hyperpolarizabilities ($\gamma$) of the title compounds has been calculated using the following expressions,

$$\mu = (\mu_x^2 + \mu_y^2 + \mu_z^2)^{\frac{1}{2}}, \quad (1)$$

$$\Delta \alpha = 2^{\frac{1}{2}} \left[ (\alpha_{xx} - \alpha_{yy})^2 + (\alpha_{yy} - \alpha_{zz})^2 + (\alpha_{zz} - \alpha_{xx})^2 + 6\alpha_{xx}^2 + 6\alpha_{yy}^2 + 6\alpha_{zz}^2 \right]^{\frac{1}{2}}, \quad (3)$$

and,

$$\langle \gamma \rangle = \frac{1}{5} \sum_{i,j=x,y,z} \left( \gamma_{ij} + \gamma_{ji} + \gamma_{ij} \right). \quad (4)$$

In the present work as the optical dispersion in the medium was not taken into account, the average (or absolute value) of static second hyperpolarizability can be simplified via the Kleinmann, 43 approach and calculated through the expression,

$$\langle \gamma \rangle = \frac{1}{5} \left[ \gamma_{xxxx} + \gamma_{yyyy} + \gamma_{zzzz} + 2(\gamma_{xxyy} + \gamma_{yxxy} + \gamma_{yyyy}) \right]. \quad (5)$$

The average linear polarizability $\langle \alpha \rangle$ can be related with the linear refractive index ($n$) of the crystal by the Clausius-Mossotti relation, which is given by, 44

$$\frac{n^2 - 1}{n^2 + 2} = \frac{4\pi N}{3} \langle \alpha \rangle, \quad (6)$$

where $N$ is the number of molecules per unit cell volume. The experimental quantity, the third-order electric susceptibility $\chi^{(3)}$, is related to the second hyperpolarizability by the expression, 44, 45

$$\chi^{(3)} = f^4 N \langle \gamma \rangle, \quad (7)$$

where $f$ is the Lorentz local field correction factor given by,

$$f = \frac{(n^2 + 2)}{3}. \quad (8)$$
All the numerical results for the tensors polarizability and hyperpolarizabilities were obtained from the Gaussian-09 output file and converted by the electronic units (esu), where the molecular environment were taken into account through the SM method.

3. Results and Discussion

3.1. FT-IR Computational Studies

The characteristic vibrational modes and functional groups present in CAD were analyzed by Fourier Transform Infrared Spectrum (FT-IR). The spectrum was recorded in the range of 400–4000 cm⁻¹. From Figure 4 we observed that a transmittance peak appears at 3806 cm⁻¹ which is due to OH stretching vibration. The C-H stretching vibration is observed at 3128 and 3055 cm⁻¹. The stretching vibration O-C occurs in 1829, 1387 and 1178 cm⁻¹ respectively. The peak 1301 cm⁻¹ is attributed to H-C-C stretching vibration; peak 702 cm⁻¹ is the H-C-C bending, and the 586 cm⁻¹ peak is attributed to the H-O-C-C torsion movements. Thus, all functional groups present in the crystalline structure of CAD were confirmed.

Figure 4: CAM-B3LYP/6-311++G(d,p) used to calculate FT-IR spectrum of C₅H₈O₂.

3.2. Hirshfeld Surface Analysis

The molecular structure CAD, C₅H₈O₂, previously studied by Tim Peppel et al., was analyzed in this work using the Hirshfeld surface (HS) and its associated 2D-fingerprint plot. The calculate were made using in Density Functional Theory (DFT) at level Becke88/LYP/6-311G(d,p) to experimental X-ray diffraction data via Tontto. The HS and its 2D-fingerprint figures allow us visualizing, exploring and quantifying the intermolecular interactions in the crystalline network of the compound CAD. The surface was generated on the basis of the normalized contact distances, which are defined in terms of $d_i$ (the distance to the nearest nucleus within the surface) and $d_e$ (the distance from the point to the nearest nucleus external to the surface) related to van der Waals radii. The high resolution default of $d_{norm}$ surface was mapped over the colour scale, ranging from −0.369 (red) to 1.201 Å (blue), with the fingerprint plots using the expanded 0.6–2.8 Å view of $d_{esr}$, $d_i$, Figure 5, where a surface with a blue-white-red scheme is showed. The blue spots are devoid of close contacts, the white areas represent contacts around the van der Waals radius and the red regions evidence shorter contacts. The Hirshfeld surface analysis of CAD confirms that the molecules are linked into centrosymmetric dimers via pairs of O–H...O hydrogen bonds in the crystals. The distance O···H is 1.635 Å (see Figure 5). The 2D-fingerprint plots (Figure 6) derived from $d_i$ and $d_e$ from pairs measured on each individual point of the calculated HS summarize the contributions of intermolecular contacts to the total surface area of Hirshfeld. The intermolecular contacts that can be explored in CAD are as follows: C···C, C···H, C···O, H···H and H···O. The intercontacts H···O the figure 6 (fingerprint) presents characteristic peaks that provide evidence of non-classical hydrogen bonding, including reciprocal contacts with 34.3% of the total surface. The contacts of type H···H show the highest contributions with a total of 52.5% followed by C···H (8.7%), C···C (2.5%) and C···O (1.6%).

Figure 5: The Hirshfeld surface $d_{norm}$ mapped of C₅H₈O₂ for visualizing the intercontacts, showing molecules are linked into centrosymmetric dimers via pairs of O–H...O hydrogen bonds.

3.3. Static Electrical Parameters

Computational Calculation

In Table 1 our results for the components and average values of the dipole moment and the linear polarizability for the isolated molecule and embedded molecule of the CAD are presented. From Table 1 can be seen that the value of the average dipole moment is found to be 2.03D and 2.99D for the isolated and embedded molecule respectively, showing that the environment polarization effect in this case is substantial and causes an increase of 47.29% in the average dipole moment. The major contribution to the average di-
The dipole moment is given by the $\mu_x$ component, mainly for the embedded molecule. However, the values of the average linear polarizability and the linear polarizability components are practically insensible to the crystalline environment polarization. As consequence of this fact a small value of the linear polarizability anisotropy can be observed in Table 1, and $\Delta\alpha$ value are smaller for the embedded molecule ($2.6 \times 10^{-24}$ esu) than for the isolated molecule ($3.2 \times 10^{-24}$ esu). And as can be seen the diagonal component dominates the polarizability and are the elements responsible by the calculation of the average linear polarizability (equation 2).

In Table 2 the CAM-B3LYP/6-311++G(d,p) results for the second hyperpolarizability (in units of $10^{-36}$ esu) for the static case are presented for CAD isolated and embedded molecules. As shown in the Table 2 the values of the average second hyperpolarizability (in units of $10^{-36}$ esu) are 5.39 and 4.77 for isolated molecule and embedded molecule respectively. Although the values of the average dipole moment and average linear polarizability for the CAD were two and three times the urea values respectively, the values of average second hyperpolarizability are found almost similar to urea ($4.16 \times 10^{-36}$ esu) and smaller than the value for the L-arginine phosphate monohydrate crystal ($14.16 \times 10^{-36}$ esu).

The calculations for the linear refractive index ($n$) via Eq. (6) and $\chi^{(3)}$ through Eq. (7) were calculated using the DFT/CAM-B3LYP functional and 6-311++G(d,p) basis set. In these calculations we have used the static value of the electric parameters (Table 2). In a more recent work the SM approach was used to simulate the linear refractive index and the third-order electric susceptibility of the (2E)-3-(3-methylphenyl)-1-(4-nitrophenyl)prop-2-en-1-one (3MPNP) crystal with results close to the experimental ones. The CAM-B3LYP results for the linear refractive index and the static third-order non-linear susceptibility, $n = 1.47$ and $\chi^{(3)} = 17.84 \times 10^{-22}$ (m-V). It is worth noting that this approach is an approximation to estimate the NLO properties and other factors can also affect the NLO responses. Also, in Table 2 the percentage variation of the second hyperpolarizabilities tensor components is shown: note that all values are reduced due to the influence of the environment polarization.

The Table 3 shows the influence of environment polarization on the electron density of the CAD molecule due to the field of punctual charges of neighboring molecules that can also be qualitatively analyzed in terms of partial atomic charges. The results of the charges fit via...

<table>
<thead>
<tr>
<th>Isolated</th>
<th>Embedded</th>
<th>$\mu_x$</th>
<th>$\mu_y$</th>
<th>$\mu_z$</th>
<th>$\mu_\rho$</th>
<th>$\Delta\alpha$</th>
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<td>$\alpha_{xx}$</td>
<td>9.28</td>
<td>9.36</td>
<td>-1.82</td>
<td>-1.91</td>
<td>-0.21</td>
<td>2.03</td>
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<td>$\alpha_{xy}$</td>
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<td>-0.36</td>
<td>2.03</td>
</tr>
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<td>$\alpha_{xz}$</td>
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<td>-0.29</td>
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<td>-2.18</td>
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<td>$\alpha_{yz}$</td>
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<td>9.10</td>
<td>2.03</td>
<td>2.03</td>
<td>2.03</td>
<td>2.03</td>
</tr>
<tr>
<td>$\alpha_{zz}$</td>
<td>9.06</td>
<td>9.09</td>
<td>2.03</td>
<td>2.03</td>
<td>2.03</td>
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<tr>
<td>$\Delta\alpha$</td>
<td>3.21</td>
<td>3.01</td>
<td>1.68</td>
<td>1.68</td>
<td>1.68</td>
<td>1.68</td>
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</table>

Table 2: CAM-B3LYP/6-311++G(d,p) results for the second hyperpolarizability (in $10^{-36}$ esu) in the static case.

<table>
<thead>
<tr>
<th>$C_3H_8O_2$</th>
<th>$\gamma_{xxxx}$</th>
<th>$\gamma_{yyyy}$</th>
<th>$\gamma_{zzzz}$</th>
<th>$\gamma_{xxyy}$</th>
<th>$\gamma_{yyzz}$</th>
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<th>$\gamma_{yyzz}$</th>
<th>$\gamma_{xxzz}$</th>
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</thead>
<tbody>
<tr>
<td>Isolated</td>
<td>4.80</td>
<td>5.04</td>
<td>4.52</td>
<td>2.71</td>
<td>1.87</td>
<td>1.70</td>
<td>5.39</td>
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<tr>
<td>Embedded</td>
<td>5.40</td>
<td>5.44</td>
<td>5.69</td>
<td>3.26</td>
<td>1.50</td>
<td>1.56</td>
<td>4.77</td>
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<tr>
<td>$\Delta%$</td>
<td>-6.25</td>
<td>-11.90</td>
<td>-18.36</td>
<td>-5.54</td>
<td>-19.79</td>
<td>-8.24</td>
<td>-11.50</td>
<td></td>
<td></td>
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</tbody>
</table>
CHELPG for the isolated and embedded molecules show a small charge transfer between H1-O1-C1-O2 of the isolated molecule (0.026e) for the embedded molecule (–0.022e). The compound methyl (C5-H5A-H5B-H5C) reduced its charge by around 161%.

Table 3: MP2/6-311+G(d,p) results for the CHELPG atomic charges of isolated and embedded CAD.

<table>
<thead>
<tr>
<th>Number</th>
<th>Atom</th>
<th>Isolated Charge (e)</th>
<th>Converged Charge (e)</th>
<th>∆%</th>
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<tbody>
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<td>1</td>
<td>C1</td>
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<tr>
<td>2</td>
<td>C2</td>
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<td>–0.345</td>
<td>–0.71</td>
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<td>3</td>
<td>H2</td>
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<td>0.168</td>
<td>–6.50</td>
</tr>
<tr>
<td>4</td>
<td>C3</td>
<td>–0.103</td>
<td>–0.099</td>
<td>–3.25</td>
</tr>
<tr>
<td>5</td>
<td>H3</td>
<td>0.115</td>
<td>0.155</td>
<td>34.89</td>
</tr>
<tr>
<td>6</td>
<td>C4</td>
<td>0.229</td>
<td>0.178</td>
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<tr>
<td>7</td>
<td>H4A</td>
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<td>–0.008</td>
<td>–66.43</td>
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<td>8</td>
<td>H4B</td>
<td>–0.038</td>
<td>–0.014</td>
<td>–63.54</td>
</tr>
<tr>
<td>9</td>
<td>C5</td>
<td>–0.054</td>
<td>–0.032</td>
<td>–22.62</td>
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<td>10</td>
<td>H5A</td>
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<td>0.019</td>
<td>100.00</td>
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<tr>
<td>11</td>
<td>H5B</td>
<td>0.015</td>
<td>0.010</td>
<td>–29.69</td>
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<td>12</td>
<td>H5C</td>
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<tr>
<td>13</td>
<td>O1</td>
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<td>–0.641</td>
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<td>O2</td>
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<td>–0.747</td>
<td>27.30</td>
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<tr>
<td>15</td>
<td>H1</td>
<td>0.436</td>
<td>0.480</td>
<td>9.94</td>
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</table>

4. Dynamic Effects

In this section the dynamic effects of an applied electric field with frequency ω is taken into account in the calculation of the dynamic properties of the carboxylic acid derivative (CAD). Using the CAM-B3LYP/6-311+G(d) we calculate the second hyperpolarizability γ(–ω; ω, 0, 0) associated to the nonlinear optical process of the intensity dependent refractive index (IDRI) from dc-Kerr result, and (2) the third harmonic generation hyperpolarizability γ(–3ω; ω, ω, 0). Following a previous work54, for small frequencies average hyperpolarizabilities can be written as,

\[ \langle \gamma(-\omega; \omega_1, \omega_2, \omega_3) \rangle \approx 2\langle \gamma(-\omega; \omega, 0, 0) \rangle - \langle \gamma(0; 0, 0, 0) \rangle. \] (9)

\[ \langle \gamma(-3\omega; \omega, \omega, \omega) \rangle \approx 6\langle \gamma(-\omega; \omega, 0, 0) \rangle - 5\langle \gamma(0; 0, 0, 0) \rangle. \] (10)

Figure 7 shows the calculated values for the average linear polarizability α(–ω; ω) and for the average second hyperpolarizabilities γ(–ω; ω, 0, 0) (Kerr effect) and γ(–2ω; ω, 0, 0) (dc-second harmonic generation (SHG)) as function of the applied electric field frequencies for both cases, isolated and embedded molecules. The results in Figure 7 (a,b,c) show that the dispersion relations are practically insensible to the environment polarization, and present a similar behavior, i.e., all curves increase smoothly and continuously.

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In order to make a more accurate estimative of the dynamic third-order susceptibility (χ(3)) we have used two different models for the γ-dynamic: (1) the frequency-dependent second hyperpolarizability γ(–ω;ω1,ω2,ω3) associated to the nonlinear optical process of the intensity dependent refractive index (IDRI) from dc-Kerr result, and (2) the third harmonic generation hyperpolarizability γ(–3ω;ω,ω,ω). Following a previous work55, for small frequencies average hyperpolarizabilities can be written as,

\[ \langle \gamma(-\omega; \omega_1, \omega_2, \omega_3) \rangle \approx 2\langle \gamma(-\omega; \omega, 0, 0) \rangle - \langle \gamma(0; 0, 0, 0) \rangle. \] (9)

\[ \langle \gamma(-3\omega; \omega, \omega, \omega) \rangle \approx 6\langle \gamma(-\omega; \omega, 0, 0) \rangle - 5\langle \gamma(0; 0, 0, 0) \rangle. \] (10)

Table 4 shows the results for the linear refractive index, the second hyperpolarizabilities IDRI (γ(IDRI)) and THG (γ(THG)), defined by equations (9) and (10) respectively and the respective third-order nonlinear susceptibilities χ(3) (IDRI) and χ(3) (THG), for two values of the electric field frequencies ω = 0.0428 a.u. and ω = 0.06 a.u..

Table 4: CAD embedded molecules linear refractive index and the IDRI and THG results for γ (10–36 esu) and the χ(3)(10–22 m2/V2).

<table>
<thead>
<tr>
<th>ω(a.u)</th>
<th>n</th>
<th>γ(IDRI)</th>
<th>χ(3)(IDRI)</th>
<th>γ(THG)</th>
<th>χ(3)(THG)</th>
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<tbody>
<tr>
<td>0.0428</td>
<td>1.48</td>
<td>5.31</td>
<td>20.54</td>
<td>6.39</td>
<td>24.72</td>
</tr>
<tr>
<td>0.06</td>
<td>1.49</td>
<td>5.81</td>
<td>22.86</td>
<td>7.89</td>
<td>31.05</td>
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</table>
The values of the $\chi^{(3)}$ for the CAD embedded molecule (Table 4) in both frequencies are high when compared with the results obtained for chalcone derivatives studied by the Z-scan technique by D’Silva et al. (2012).\textsuperscript{56} The value of the third-order electric susceptibility (in units of $10^{-22} \text{m}^2/\text{V}^2$) of the chalcone derivatives 4Br4MSP, 3Br4MSP and 4N4MSP are 2.30, 1.99 and 2.37 respectively\textsuperscript{56}, the CAD $\chi^{(3)}$ value is 22.86 ($\omega = 0.06$ a.u, $\lambda = 759$ nm), therefore 9.94, 11.49 and 9.65 times higher than these values respectively. The typical $\chi^{(3)}$-value reported in the literature is of order of $10^{-22}/V$.\textsuperscript{57}

### 5. Solvent Media

The solvent media may change the properties of the molecules, as the displacements of electronic absorption bands, the reaction rates, the NLO properties, among others. Thus an adequate description of the solvent medium is necessary. There are two models that simulate the solvent medium: the continuous model and the discrete model. In this work we use the method of Polarizable Continuum Model (PCM), in which the dielectric properties of the solvent medium are used for the solvation of the system. A PCM advantage is the possibility of making a purely quantum treatment of the solute-solvent interaction. The calculations were performed numerically based on finite field method, include the optimization of the structure using the PCM-CAM-B3LYP/6-311++G(d,p) level of theory. We selected Chloroform, Dichloromethane, Acetone, Ethanol, Methanol, Dimethyl Sulfoxide (DMSO), and Water as the solvent media, and the gas-phase results are included by comparison.

When in a solvent medium the electrical properties of the organic compounds change, one of the changes is the loss of the centrosymmetry conformation which causes a not null value for the first hyperpolarizability. Here we consider the first hyperpolarizability component parallel to the dipole moment (taken as z-direction) given by,

$$\beta_{lx} = \frac{1}{5} \sum_{l=1}^{3} (\beta_{lxi} + \beta_{lzi} + \beta_{li})$$

(11)

The dynamical electric parameter $\beta_{lz}(-\omega; \omega_1, \omega_2)$ is an experimentally relevant quantity because it is closely related to the direction of the ground state charge transfer. In the specific cases we consider $\beta_{lz}(-\omega; \omega, 0)$ and $\beta_{lz}(-2\omega; \omega, \omega)$ that correspond to the Pockels effect and to the SHG respectively.

Table 5, shows the values for average linear polarizability, first hyperpolarizability and second hyperpolarizability for various solvent media. Figure 8 shows that the average linear polarizability increases to a value close to 26.3% when comparing the DMSO medium with the gas-
phase. The first hyperpolarizability $\beta_{||}(-\omega; \omega, 0) \approx \beta_{||}(-2\omega; \omega, \omega)$ increases around 86.3% [65.5%] when comparing the gas-phase with water, see Figure 9, and the second hyperpolarizability $\gamma(-\omega; \omega, 0, 0) \approx \gamma(-2\omega; \omega, \omega, 0)$ increases around 59.5% [43.6%] when comparing the DMSO medium with the gas-phase, see Figure 10. The choice of the solvent medium allows us to control the NLO properties; in other words, the first hyperpolarizability is more sensitive in water whereas the second hyperpolarizability is more sensitive in DMSO solvent medium.

Figure 10: PCM-CAM-B3LYP/6-311++G(d,p) results for second hyperpolarizabilities $(10^{-36}$ esu$)$ $\gamma(-\omega; \omega, 0, 0)$ and $\gamma(-2\omega; \omega, \omega, 0)$ for $\omega = 0.04282$ a. u. of compound C$_5$H$_8$O$_2$ in a solvent medium.

Figure 11 shows the overlap of the structure of the crystal molecule with the molecule in the gas phase of the compound C$_5$H$_8$O$_2$; the anchorage point occurs in the O$_2$-C$_1$-O$_1$-H$_1$ geometry. The X-ray geometry of the theoretical structure was analyzed in terms of root mean square deviation (RMSD) calculated for non H-atoms. The H-atoms were neglected in view of their uncertainties in X-ray position refinement. The compound C$_5$H$_8$O$_2$ presents in RMSD = 0.0328 max. d = 0.0571 Å. The RMSD parameter indicates no significant deviation between the theoretical and experimental data.

Figure 11: Compound C$_5$H$_8$O$_2$ overlap of compound yellow (crystal), red (gas-phase). The anchorage point occurs in the O$_2$-C$_1$-O$_1$-H$_1$ geometry.

6. HOMO and LUMO Analysis

The PCM-CAM-B3LYP/6-311+G(d) level of theory has been used to obtain the energies of the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO). These quantum chemical parameters, HOMO and LUMO energies, play the same role of electron donor and electron acceptor, respectively; therefore they determine the molecular reactivity and the ability of a molecule to absorb light. Also they can be used for predicting the most reactive position in π-electron systems and explain several types of reactions in conjugated systems. The HOMO-LUMO separation energy is called the gap energy, and a small value of this parameter implies a charge transfer interaction within the molecule, which influences the NLO activity of the molecule. In Table 5 the HOMO and LUMO energies for the CAD in several solvent media are presented, showing that the values present a small variation in different solvent media.

<table>
<thead>
<tr>
<th>C$_5$H$_8$O$_2$</th>
<th>HOMO</th>
<th>LUMO</th>
</tr>
</thead>
<tbody>
<tr>
<td>Acetone</td>
<td>-9.22</td>
<td>-0.27</td>
</tr>
<tr>
<td>Chloroform</td>
<td>-9.22</td>
<td>-0.25</td>
</tr>
<tr>
<td>Dichloromethane</td>
<td>-9.23</td>
<td>-0.26</td>
</tr>
<tr>
<td>DiMethylSulfoxide</td>
<td>-9.23</td>
<td>-0.28</td>
</tr>
<tr>
<td>Ethanol</td>
<td>-9.23</td>
<td>-0.28</td>
</tr>
<tr>
<td>Gas-Phase</td>
<td>-9.23</td>
<td>-0.17</td>
</tr>
<tr>
<td>Methanol</td>
<td>-9.23</td>
<td>-0.28</td>
</tr>
<tr>
<td>Water</td>
<td>-9.23</td>
<td>-0.28</td>
</tr>
</tbody>
</table>

It is clear from Figure 12 that the HOMO is largely located on C2-C3 atoms and moderately on H4A-C4-H4B atoms whereas the LUMO is mainly present on C2-C3 atoms and moderately on C3 atom. Also the band gap energies in different solvent media are presented in Figure 12, where we note a small variation of this parameter is, of order of 0.1 eV. Through the HOMO and LUMO energies the global chemical reactivity descriptors (GCRD) such the electronic chemical potential ($\mu_{cp}$), the chemical hardness ($\eta$), softness ($S$), and the global electrophilicity index ($\sigma$) can be calculated through the equations:

$$\mu_{cp} = \frac{1}{2} (E_{HOMO} + E_{LUMO}),$$

(12)

$$\eta = \frac{1}{2} (E_{LUMO} - E_{HOMO}),$$

(13)

$$S = \frac{-E_{HOMO}}{2\eta},$$

(14)

$$\sigma = \frac{\mu_{cp}^2}{2\eta},$$

(15)
Calculations for the GCRD can be seen in Table 6 for various solvent media. The obtained GCRD results reveal that the CAD molecule offers good chemical strength and stability.

The effect of the solvent on the GCRD is not significant.

When we observed the effect of the transition between non-polar solvents (Chloroform) and polar solvents (DMSO) the Band-Gap between Chloroform-DMSO does not exceed 0.03 eV, indicating that this property is not significantly affected by the solvent.

### 7. Conclusion

Studies of the structural and electrical properties of (E)-pent-2-enoic acid (CAD) with structural formula C_5H_8O_2 have been performed by the Hirshfeld surface analysis and the DFT/CAM-B3LYP and MP2 theory both with the 6-311++G(d,p) basis set. The SM approach was used to simulate crystalline environment of the CAD crystal. The dipole moment, linear polarizability and second hyperpolarizabilities were calculated for CAD isolated and...
embedded molecules. For CAD embedded molecule an estimation of the linear refractive index and the third-order nonlinear susceptibility, both static and dynamic, are performed and the results compared with available experimental results. Also the effects of solvent medium on the molecular properties were considered through the PCM method, and the HOMO and LUMO energies were calculated. The band gap energies ranged from 8.95eV (DMSO) to 9.05eV (gas-phase). In addition, the global chemical reactivity descriptors were calculated and the results reveal that the CAD molecule possesses good chemical strength and stability.

The molecular structure of the CAD crystal were explored by Hirshfeld surface analysis and the associated 2D-fingerprint plots calculated using Crystal Explorer software.38,39 The intermolecular contacts that were explored are as follows: C...C, C...H, C...O, H...H and H...O. The intercontacts H...O shown in figure 6 (fingerprint) presents characteristic peaks that provide evidence of non-classical hydrogen bonding, including reciprocal contacts with 34.3% of the total surface. The contacts of type H...H show the highest contributions with a total of 52.5% followed by C...H (8.7%), C...C (2.5%) and C...O (1.6%). The vibrational modes behavior and the functional groups present in CAD were studied by FT-IR.

Our theoretical results show that the crystalline environment polarization effect on the average linear polarizability and average second hyperpolarizability is small, but the third-order susceptibility and average second hyperpolarizability is small, environment polarization effect on the average linear polarizability is 9.94, in the static and dynamic situation, but the third-order susceptibility and average second hyperpolarizability is small, environment polarization effect on the average linear polarizability is 9.94, in the static and dynamic situation.

8. References


Povzetek